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# Characterization of a Pseudo–Random Testing Technique for Analog and Mixed–Signal Built–In–Self–Test

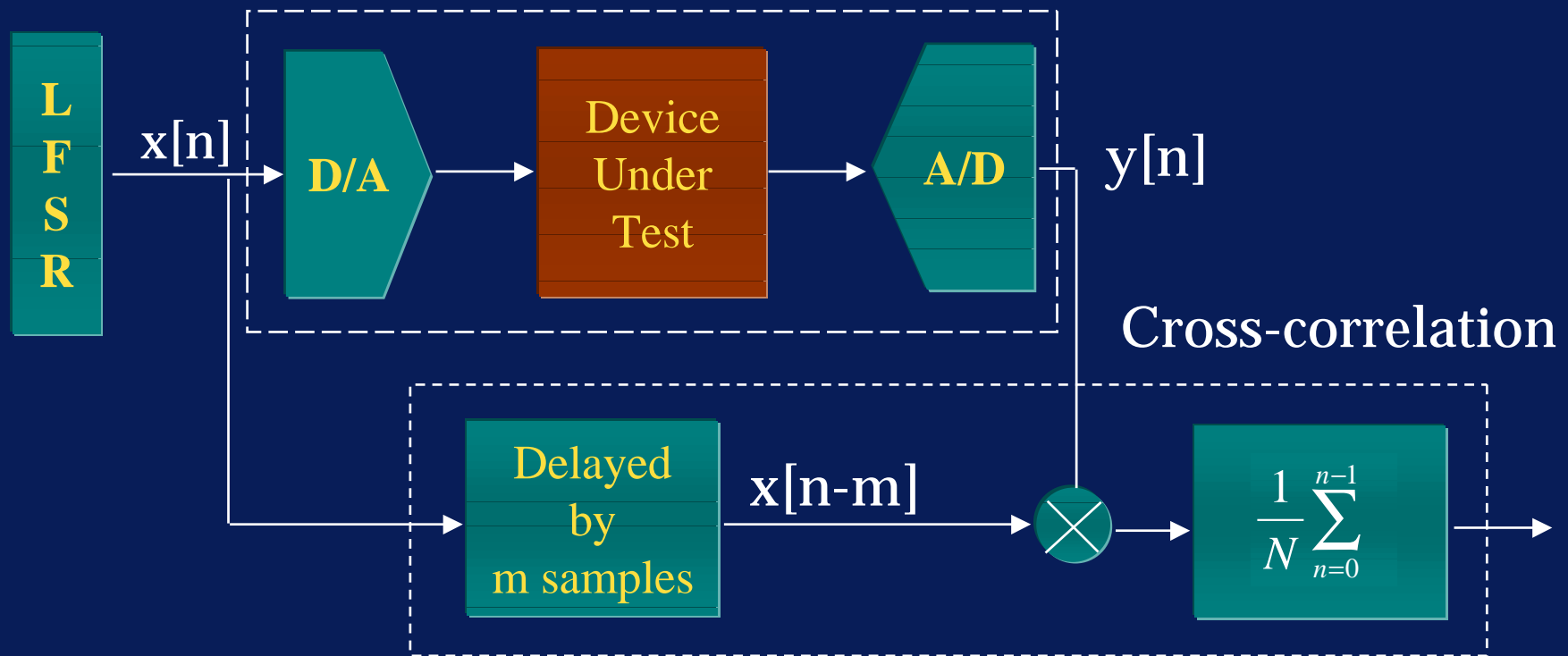
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The work was done when the first author was with Univ. of California at Santa Barbara.

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# Pseudo-Random Structure



$$\bar{\phi}_{xy}[m] = E\{x[n-m] \cdot y[n]\}$$

Ref: Pan & Cheng, ICCAD95

# Cross–Correlation Signature

Cross–Correlation is Proportional to the Impulse Response:

$$\phi_{xy}[m] = h[m] \cdot \sigma_x^2 + \mu_x^2 \cdot \sum_{k=0}^{\infty} h[k]$$

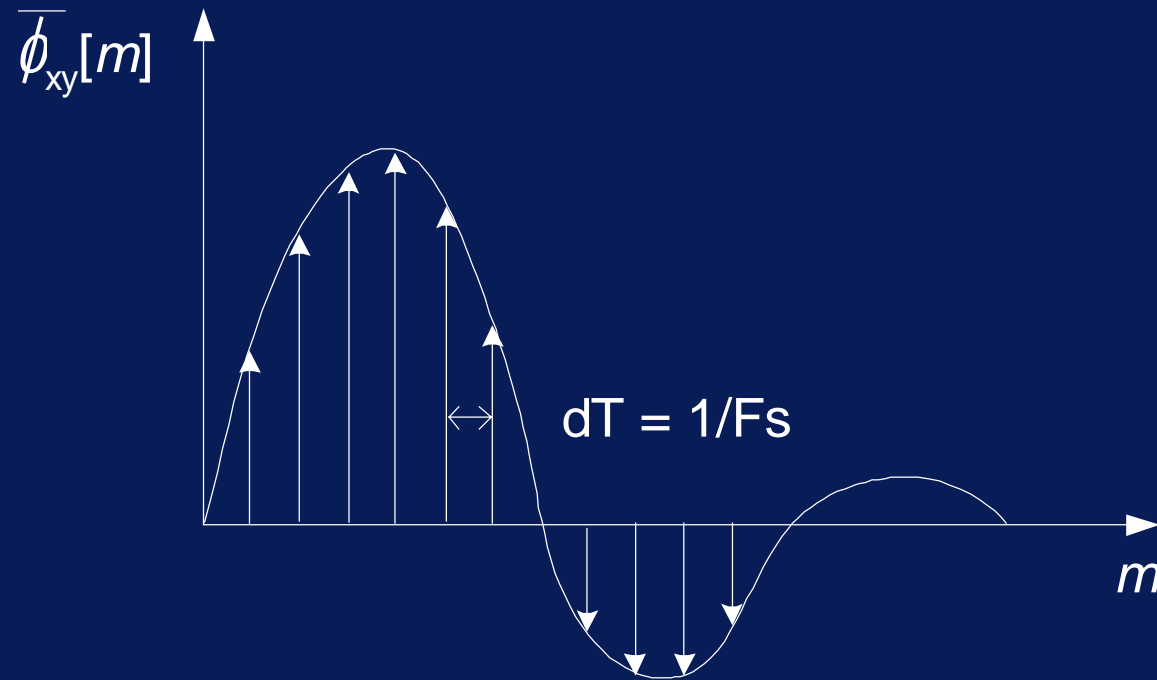
Estimated Cross–Correlation Signature Samples:

$$\bar{\phi}_{xy}[m] = \frac{1}{N} \sum_{n=0}^{n-1} x[n-m] \cdot y[n]$$

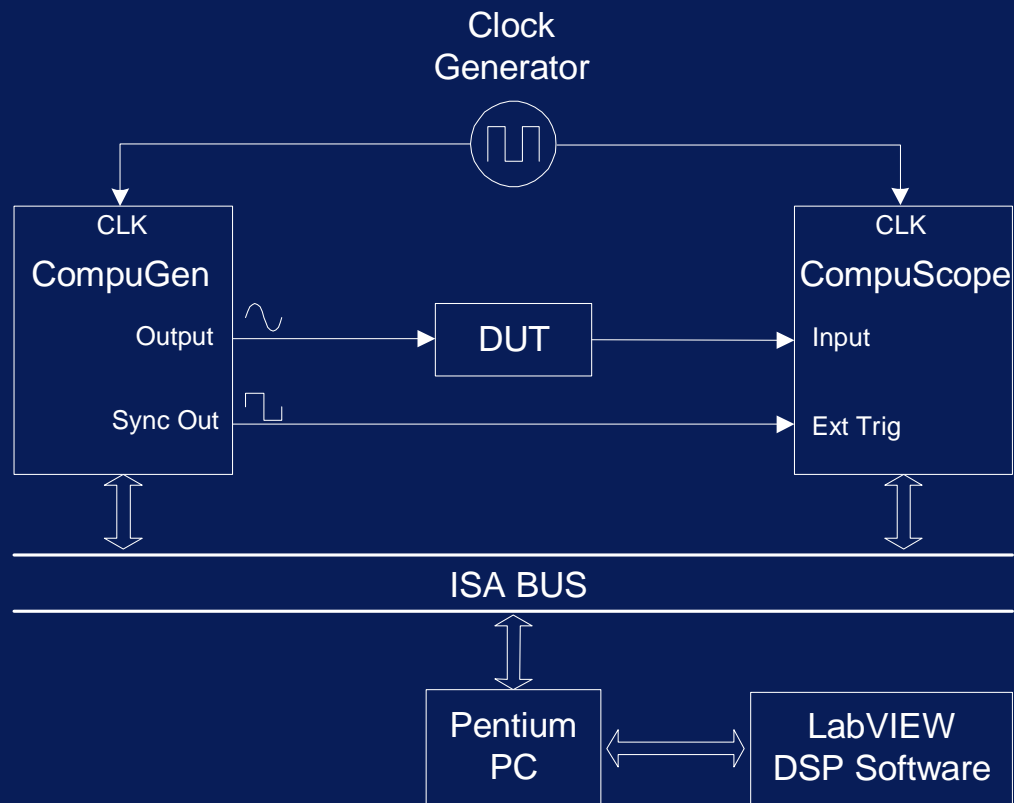
Complete Signature Set:

$$\phi = \{\bar{\phi}_{xy}[0], \bar{\phi}_{xy}[1], \bar{\phi}_{xy}[2], \bar{\phi}_{xy}, \dots, [K-1]\}$$

# Cross-Correlation Response



# Testbed Implementation



# Overview of Experimental Procedure

- Each circuit instance is generated using the Monte Carlo method.
- Pseudo-random patterns are applied to the DUT, and the cross-correlation signature samples are computed.
- A signature set is marked fault-free (faulty) if the circuit instance is within (outside) the performance boundaries.

# Test–Session Procedure

- 1) Load the pseudo–random patterns into CompuGen’s memory–buffer.
- 2) Instruct CompuGen to start continuous delivery of test–sessions.
- 3) Arm CompuScope to hardware trigger on CompuGen’s *Sync Out* signal.
- 4) When a trigger is detected, mark the starting point of the test–session.
- 5) When the current test–session has been successfully captured, transfer the response samples from CompuScope’s memory–buffer to the application software.

# Software Procedure

- 1) Adjust the values of the external resistors.
- 2) Obtain the DC offset and gain spectrum by applying a series of frequency-sweep test-sessions.
- 3) Perform a test-session based on the pseudo-random test patterns to obtain the phase spectrum and cross-correlation.
- 4) Check if the circuit instance of the DUT satisfies/violates the performance parameters
- 5) mark the cross-correlation signature set fault-free/faulty, and log the results to file.

# Classification of Circuit Instances

- Generate circuit instances collectively called a *training set*
- Carefully select 2 cross-correlation signatures
- Derive a polygon based on the convex hull function that encloses all fault-free circuit instances
- Generate circuit instances collectively called an *evaluation set*
- An instance in the *evaluation set* is classified as fault-free (faulty) if it falls within (outside) the boundaries established by the polygon.

# Classification Accuracy

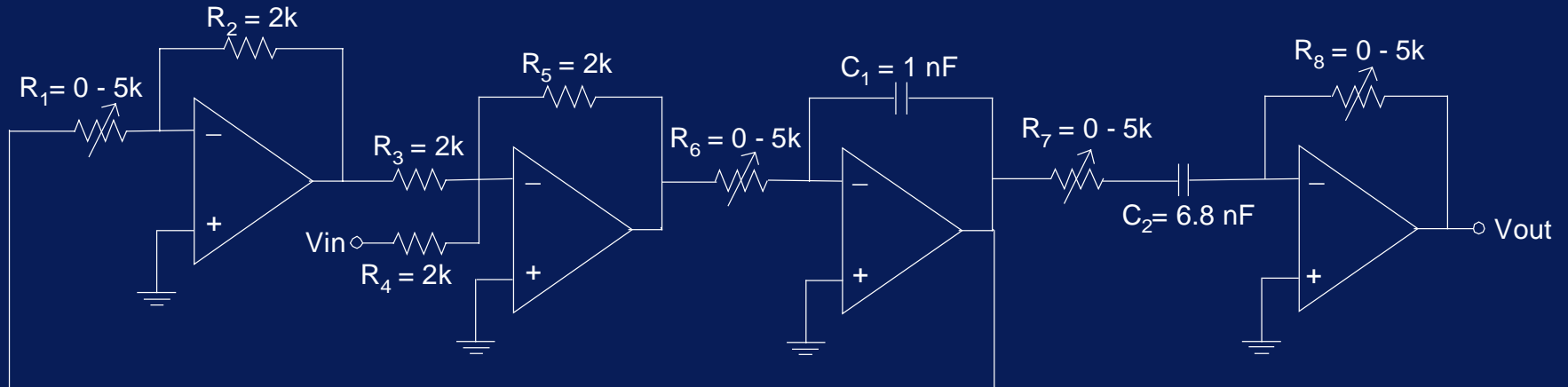
- Yield Coverage (Y):

The number of instances correctly classified as fault-free divided by the total number of known fault-free instances.

- Fault Coverage (F):

The number of instances correctly classified as faulty divided by the total number of known faulty instances in.

# Experiment: Bandpass Filter

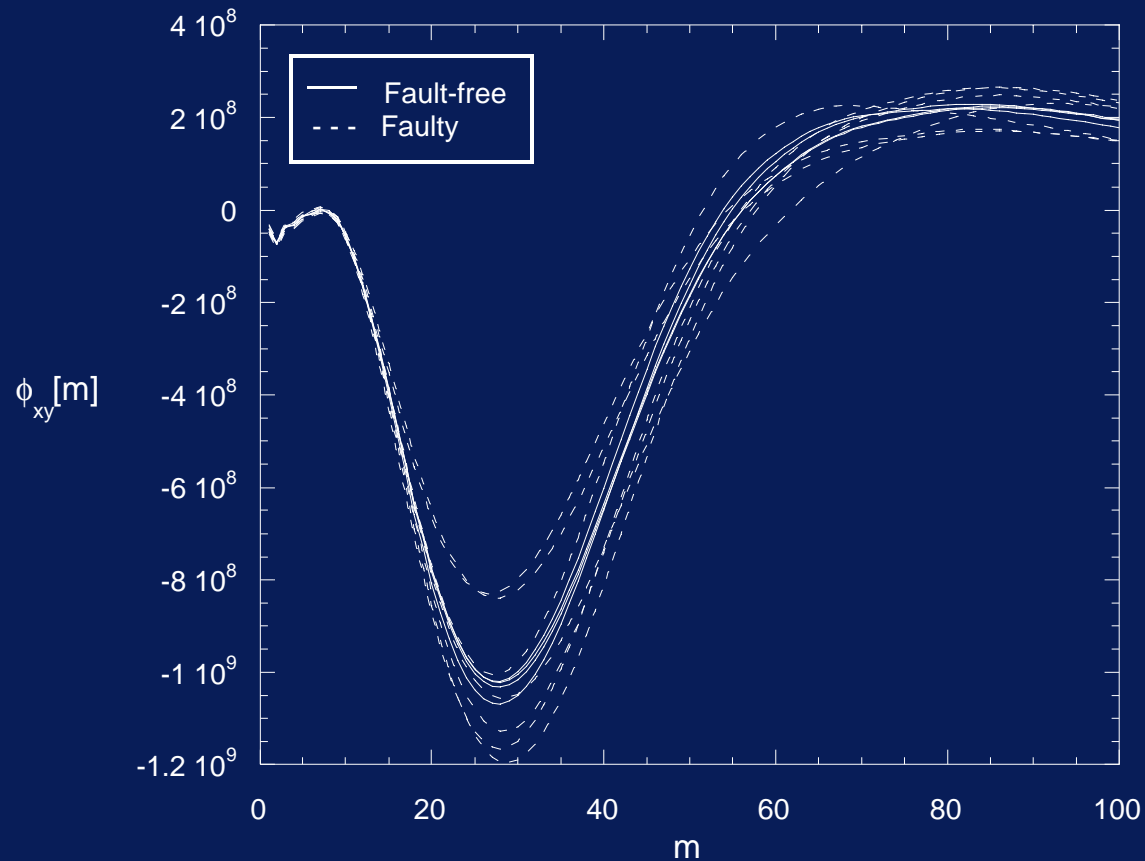


Performance parameter constraints:

- Pass-band gain (50 kHz – 200 kHz):  $-1.5 \text{ dB} \leq A_0 \leq 1.5 \text{ dB}$ .
- Stop-band attenuation:  $A_0 \leq -8 \text{ dB}$  at 10 kHz and 200 kHz.
- Pass-band phase margin:  $\phi \leq 5^\circ$ .
- DC offset in pass-band:  $V_{os} \leq 2.4 \text{ mV}$ .

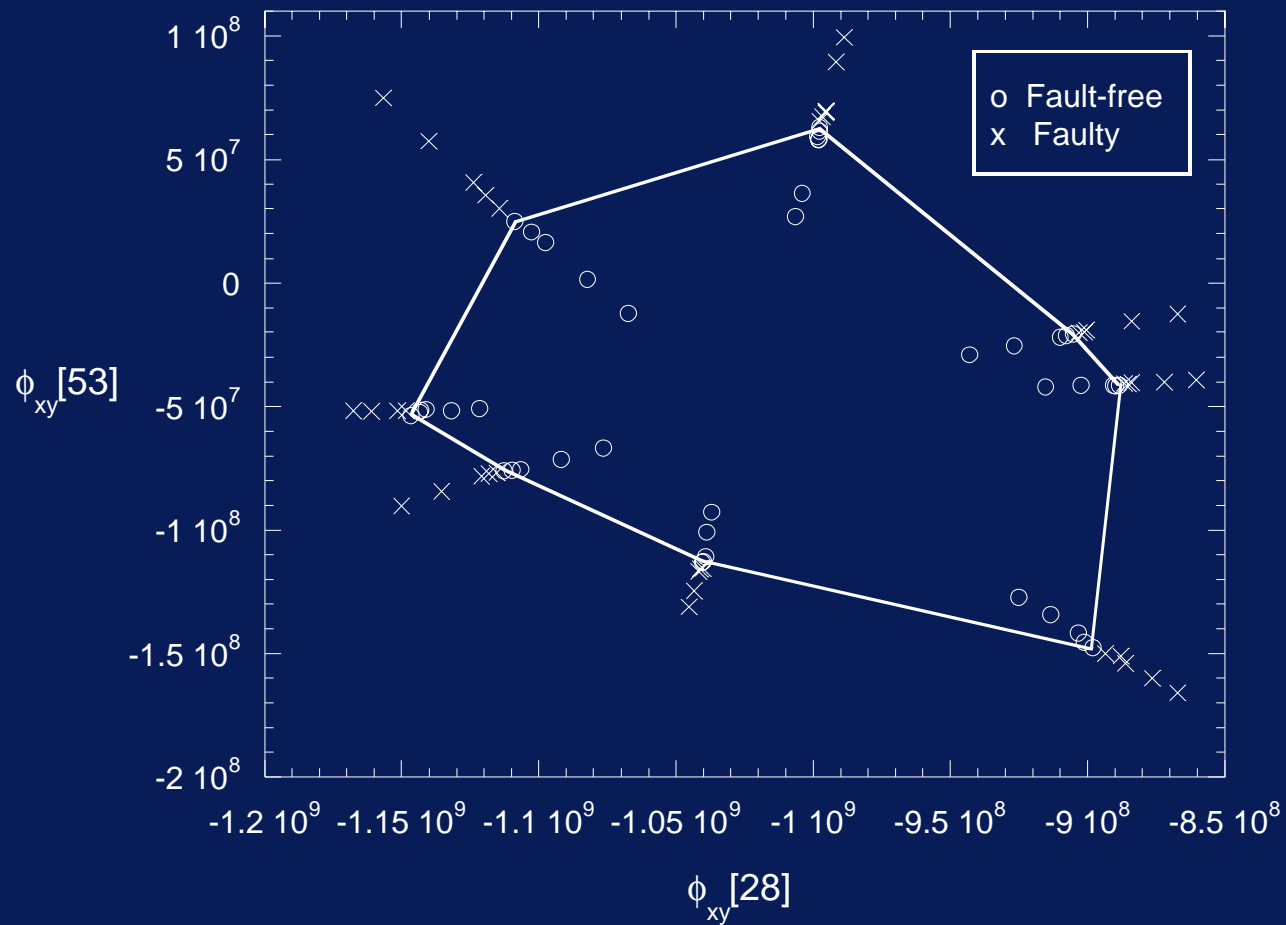
# Cross-Correlation Response Curves

Select 2 cross-correlation samples (signature-pair)



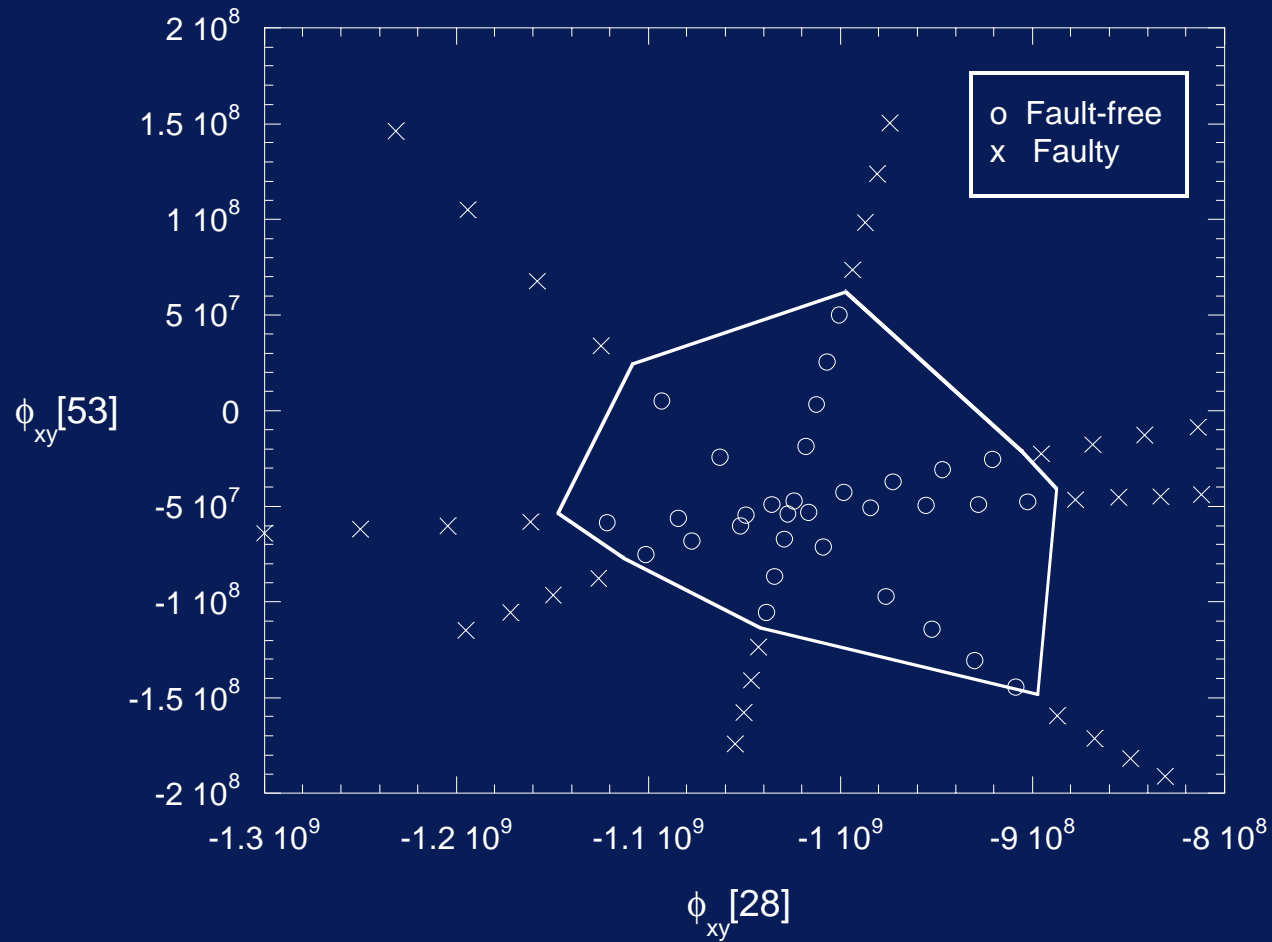
# Training Set

Derive classification boundaries to enclose all fault-free instances



# Evaluation Set

Apply classification boundaries to the evaluation set



# Results: Bandpass and Lowpass Filters

- Noise does not seem to affect the classification accuracy
- Several Signature-pairs give 100% yield and fault coverage

<i>n</i>	Bandpass Filter		Lowpass Filter	
	Noise (%)	Signature-pairs (%)	Noise (%)	Signature-pairs (%)
1	0.070	7.2	0.137	1.4
4	0.026	7.2	0.048	1.5
9	0.017	6.6	0.029	1.7
16	0.015	5.7	0.022	1.7
25	0.013	6.6	0.019	1.8

# Practical BIST Implications

- Digital on-chip test stimulus and signal analysis covering the complete frequency spectrum
- Area efficient if D/A and A/D converters are available in the design
- Cross-correlation signatures are captured into a cross-correlation signature register (CCSR) and scanned out using only one I/O pin
- ATE verifies that the 2-dimensional representation of the signatures falls within the classification boundaries of the polygon

# Future Work

- Need to generate a larger number of circuit instances for the training and evaluation set
- Need to evaluate more complex circuits with a larger number of parametric fault sites
- Complex circuits might require more than 2 cross-correlation signatures for classification

# Application Software — User Interface

